

Modul 1
Basics in
Cryptography



Objectives of Cryptography

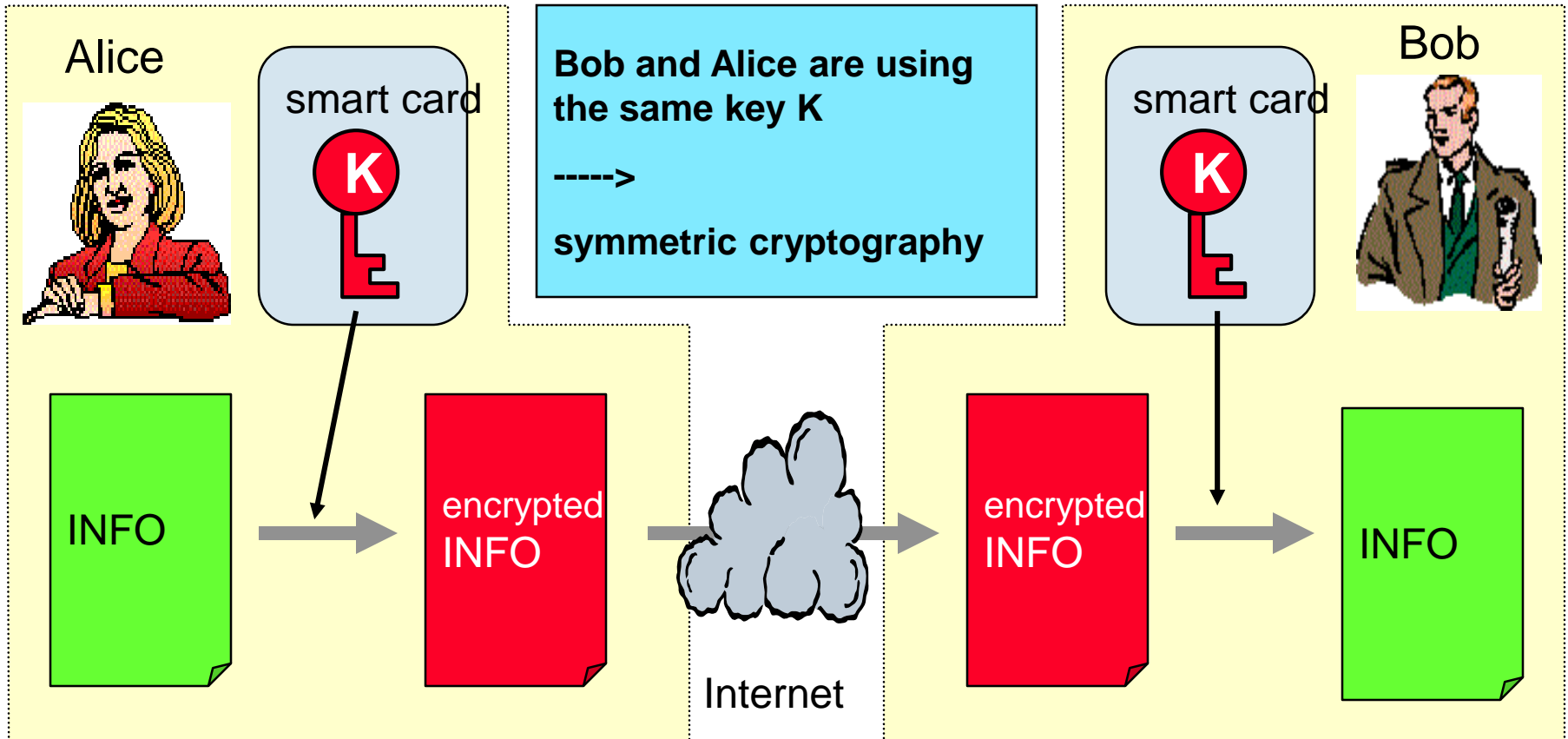
- **Privacy:**
Assure confidentiality of information
- **Integrity:**
Assure retention of information, i.e. no unauthorized modification
- **Authentication:**
Identify for certain who is communicating with you resp. verify the origin
- **Accountability:**
Assure identification who did what and when
- **No-repudiation:**
The ability to provide proof of the origin or delivery of data



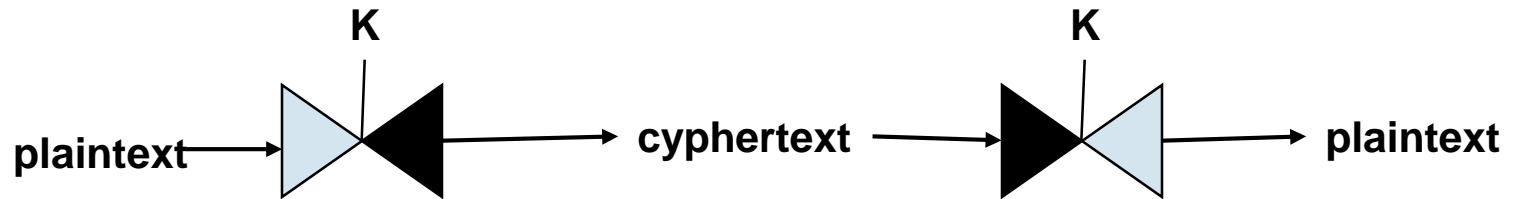
One Time Pad

- **Random Numbers + linking by XOR**
- **pros: provable safety**
- **cons: Key exchange, there are no random numbers**
- **Application case: TAN-method in the context of Home banking**

Symmetric Cryptography



Symmetric block encryption - symmetric cryptography



Let K be a Key and **enc** and **dec** a encryption function such that

$$\mathbf{dec} = \mathbf{enc}^{-1}$$

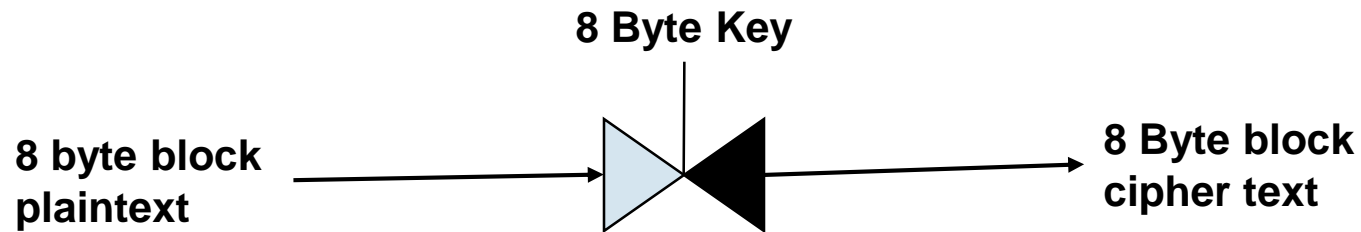
then

$$\text{plaintext} = \mathbf{dec}(K, \mathbf{enc}(K, \text{plaintext}))$$

key space (set of all keys) has elements
(this implies a key length up to bit)

→ there are approximately infinite methods to construct a symmetric block encryption algorithm

The symmetric block encryption algorithm DES



- Currently DES is the most important symmetric block encryption algorithm.
- To be honest: only 56 bit of the DES 8 Byte key is used.
- A saver variant of DES is Triple-DES (112 bit key).
- In the future the DES algorithm will be substituted by the recent AES (Advanced Encryption Standard) algorithm.
- DES is a very fast algorithm and it can easily be hardware-implemented in a smart card (crypto processor unit)
- Other block encryption algorithms:
IDEA (used by PGP, 128 key length), Blowfish, Twofish, RC2, RC5, RC6



DES and Triple-DES

- DES key
- DES encryption
- DES decryption
- formula
- Triple DES encryption
 $k = (kl, kr)$
- Triple DES decryption

$$k = (k_1, \dots, k_{56}) \in \{0,1\}^{56}$$

$$E^1_k : \{0,1\}^{64} \rightarrow \{0,1\}^{64}$$

$$D^1_k : \{0,1\}^{64} \rightarrow \{0,1\}^{64}$$

$$E^1_{(k_1, \dots, k_{56})} = D^1_{(k_{56}, \dots, k_1)}$$

$$E^3_k := E^1_{k_l} \circ D^1_{kr} \circ E^1_{kl}$$

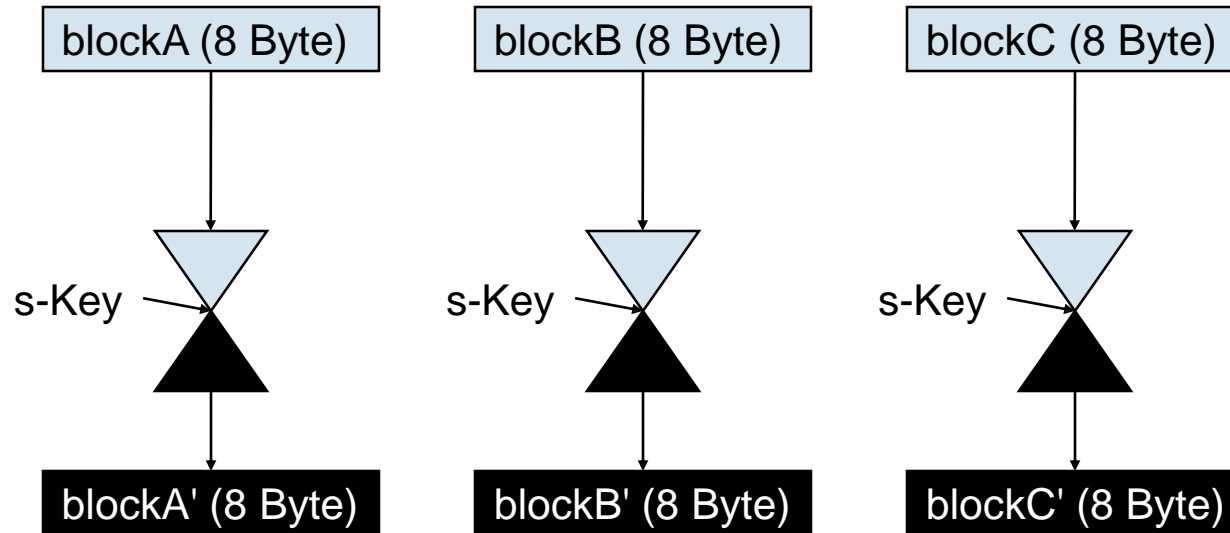
$$D^3_k := D^1_{k_l} \circ E^1_{kr} \circ D^1_{kl}$$



AES (Advanced Encryption Standard)

- in October 2000, the NIST (National Institute of Standards and Technology) announced the approval of a new secret key cipher standard chosen among 15 candidates
- block and key length of 128, 192 or 256
- Very high encryption speed (200 MBit/sec using a 1GB-PC)
- Very efficiently to implement (even on a 8-Bit smart card (math. calculation is based on the Galois field (\rightarrow 8 bit numbers)).
- Universally applicable: One way hash, MAC, pseudo random number generator
- AES can also be used by smart cards

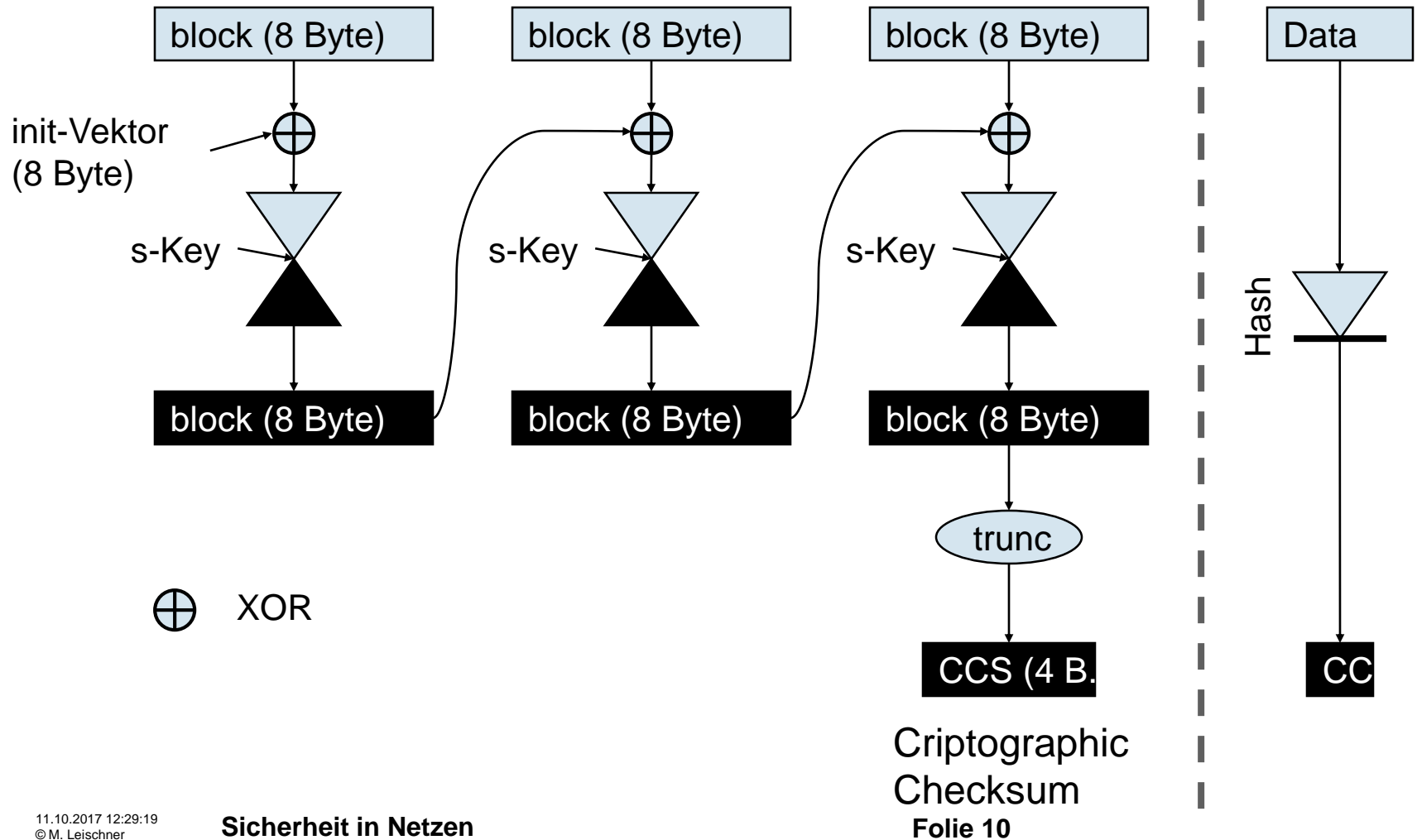
Operating Mode Electronic Code Book (ECB)



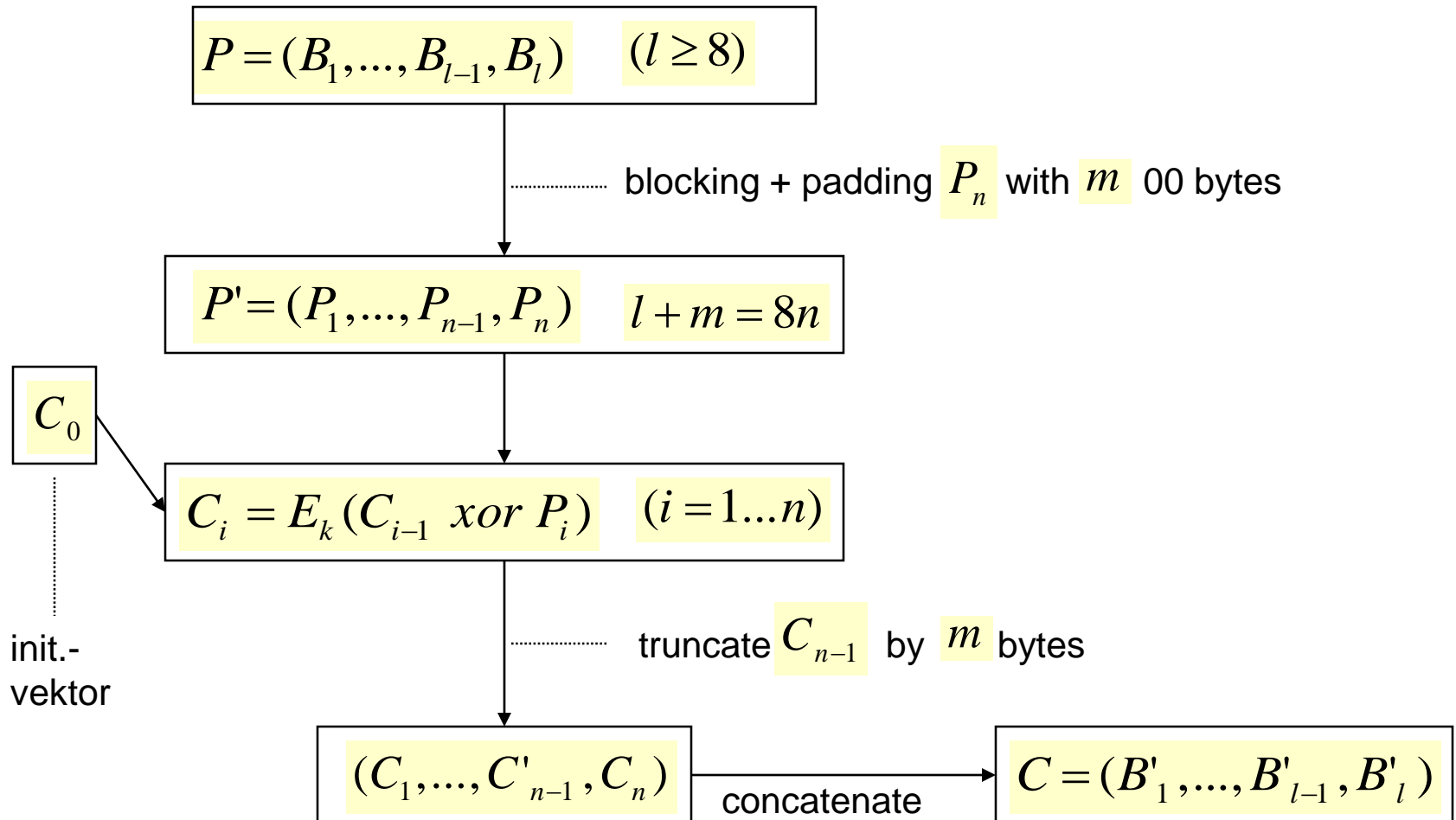
- very simple
- It is not very safe:
If block A equals block B then also the cipher blocks A' and B' are equal.



Operating Mode Cipher Block Chain (CBC) and Hashing



cipher block chaining (used by the BasicCard)





Hochschule
Bonn-Rhein-Sieg

Prof. Dr. Martin Leischner
Netzwerkssysteme und TK

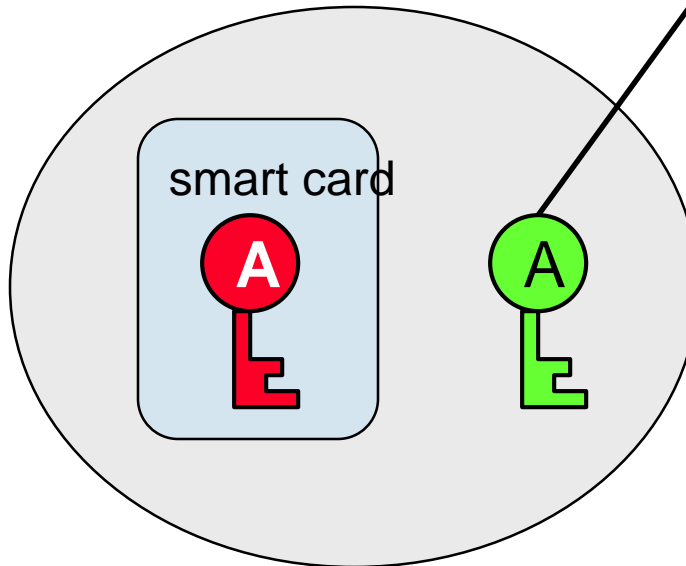
Public Key Cryptography



Public-Key-Kryptographie

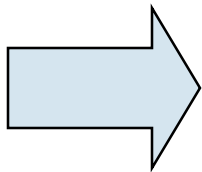


Alice



Alice has two keys

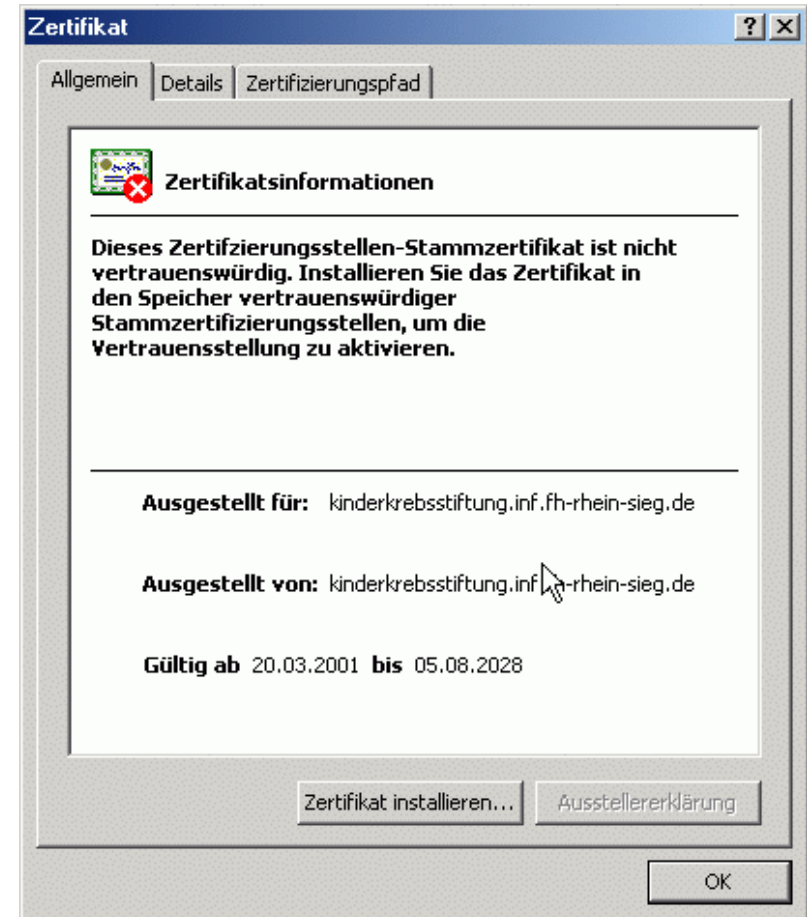
- a **secret key**
(e.g. on a smart card)
- a **public key**
(not secret, can be stored
in a public directory or on
her homepage)



To encrypt **and** decrypt information, you need **both** keys

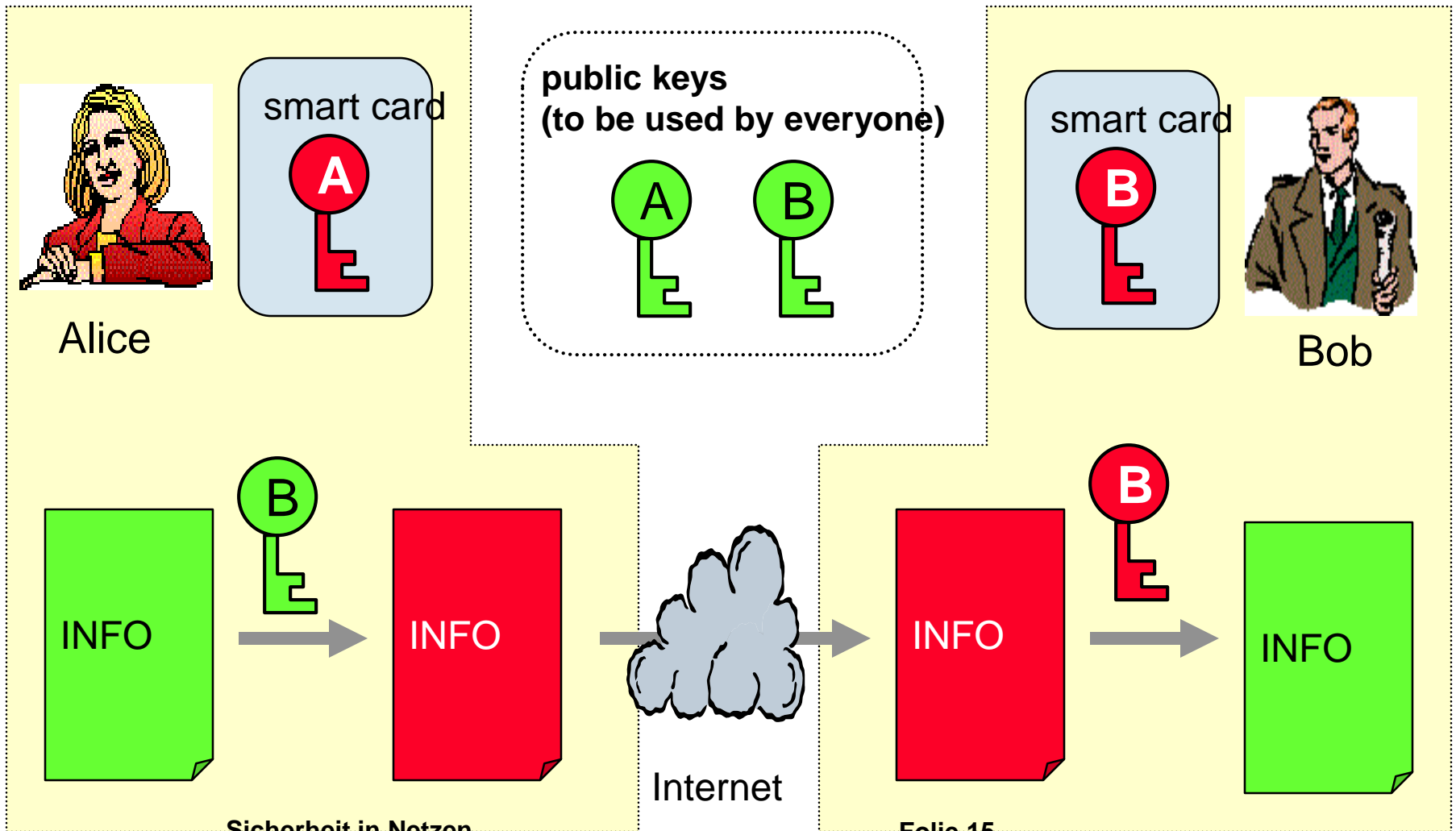
Certificate

- Tuple (owner, public key, SignatureCA(owner, public key))
- Additional data: Angabe des eingesetzten Signaturverfahrens, Beginn und Ende der Gültigkeit, Seriennummer, Attribute, Namen der ausstellenden Certification Authority, Einschränkungen der Nutzung des Signaturschlüssels
- Time Stamp
=SignatureCA (hash value, time)
- Standard: X509v3



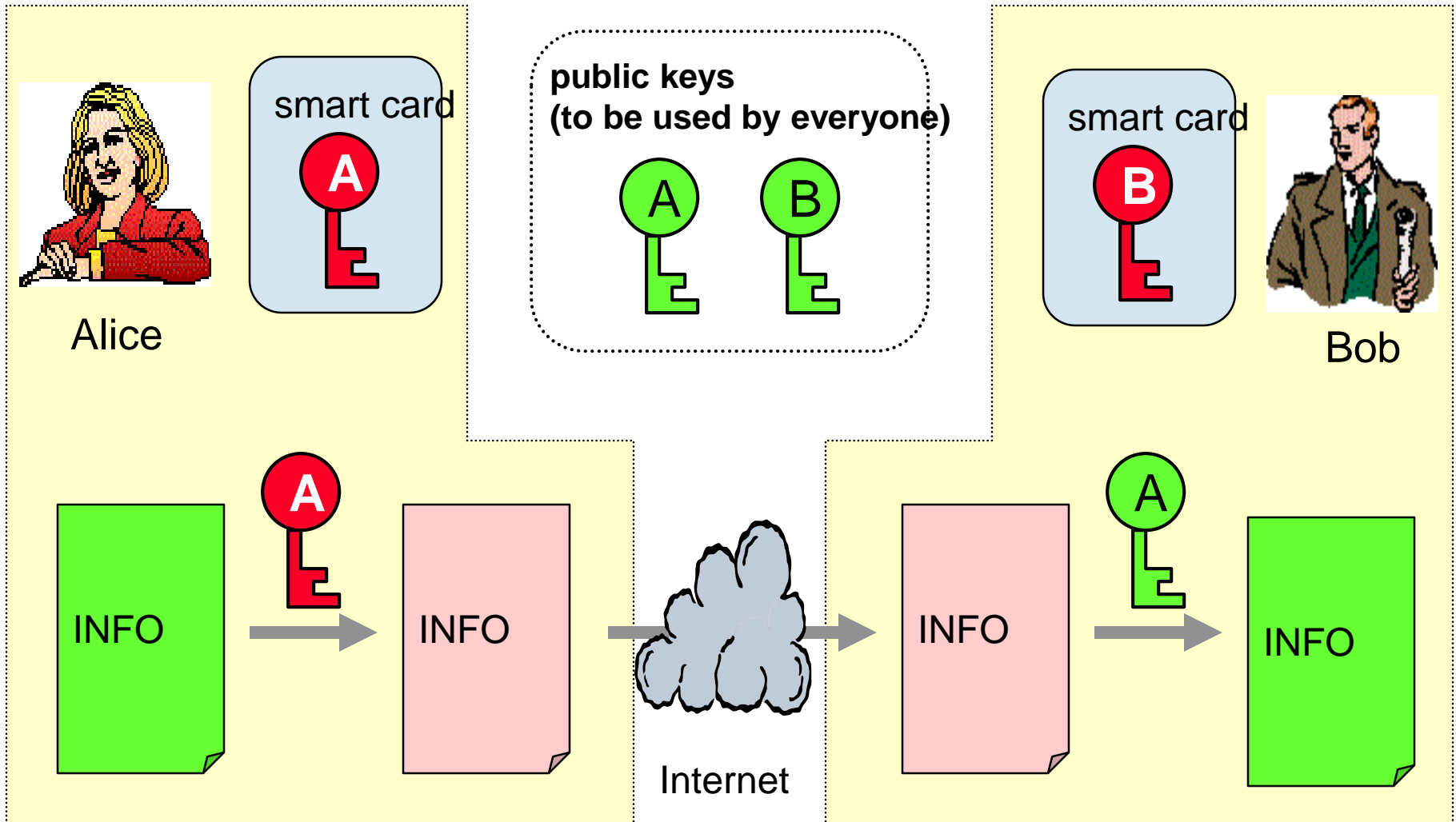


Public Key Cryptography - The Concept of Confidentiality





Public Key Cryptography - The Concept of Digital Signatures





Public Key Algorithms

RSA

- based on prime numbers
- typical key length: 1024 bit

Elliptic functions

- based on elliptic functions and finite fields
- typical key length: 160 bit

Pro and cons of public key cryptography:

- + allows sophisticated key management
- + very high safety
- slow algorithms



RSA

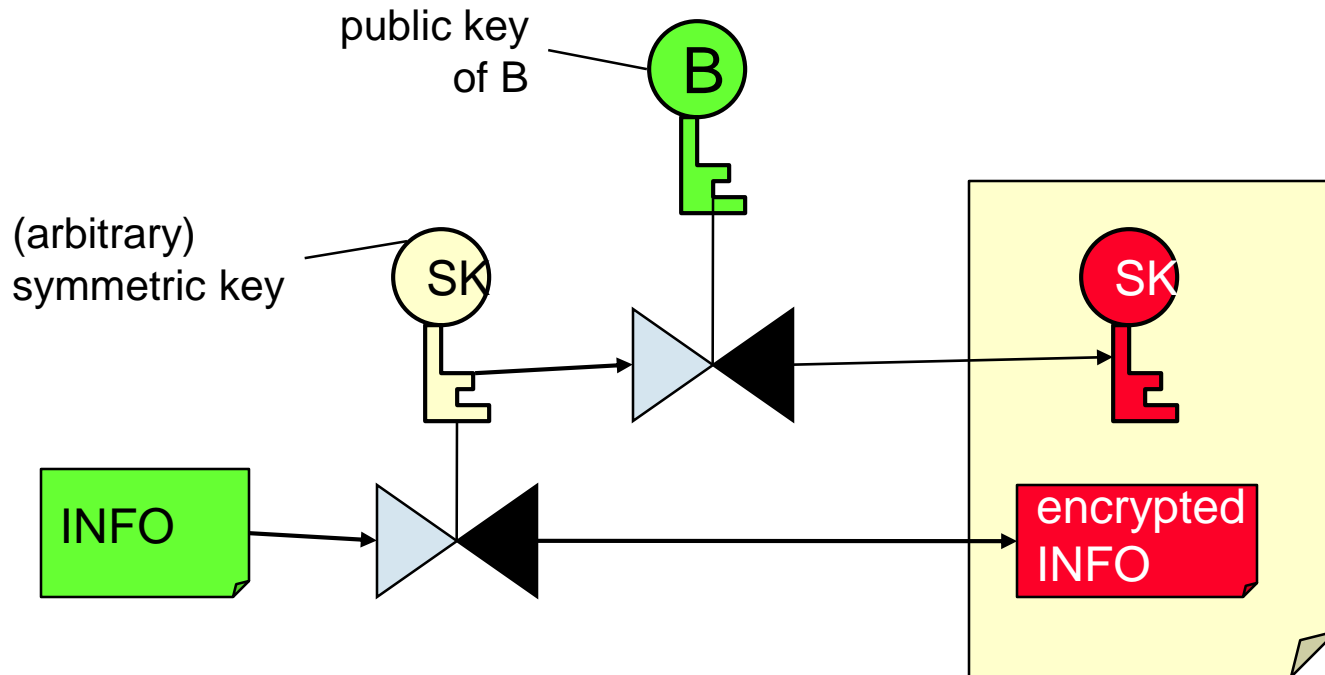
- **Method**
public key = (e,n)
private key = (d,n) , where $d \equiv e^{-1} \pmod{\varphi(n)}$ with $\varphi(n) = (p-1) * (q-1)$
encryption: plain text $M (<n) \rightarrow$ cipher text $C = M^e \pmod n$
decryption: cipher text $C \rightarrow$ plain text $M = C^d \pmod n$
- no patent (since autumn 2000)
- **Convention:**
pk: public key, encryption key
sk: signature key, secret key, private key, decryption key



Hybrid Encryption

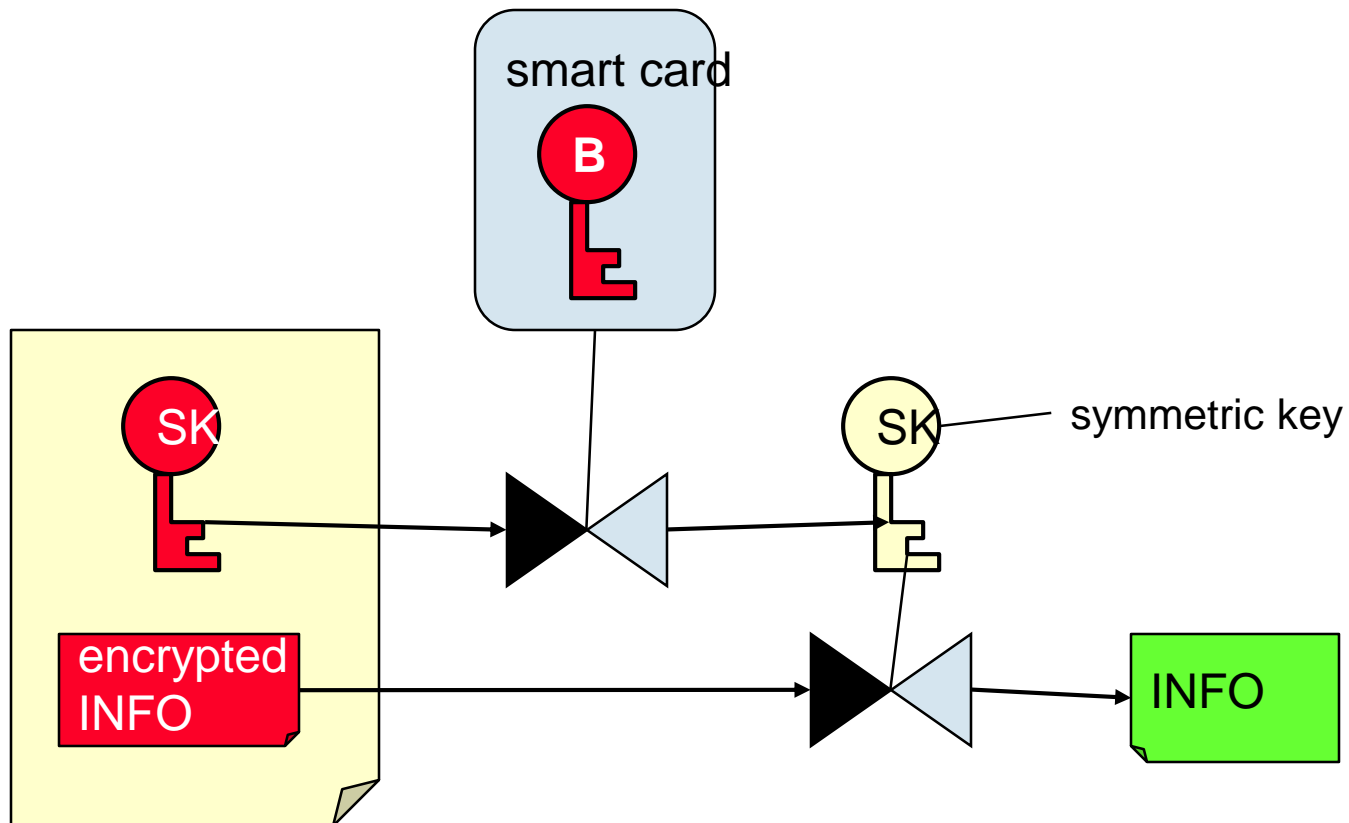
The Concept of Hybrid Encryption

Scenario: A (Alice) wants to encrypt a document INFO for B (Bob)



The Concept of Hybrid Decryption

Scenario: B (Bob) wants to read the document sent by A (Alice)





The Problem of Key Management

The problem of key management:

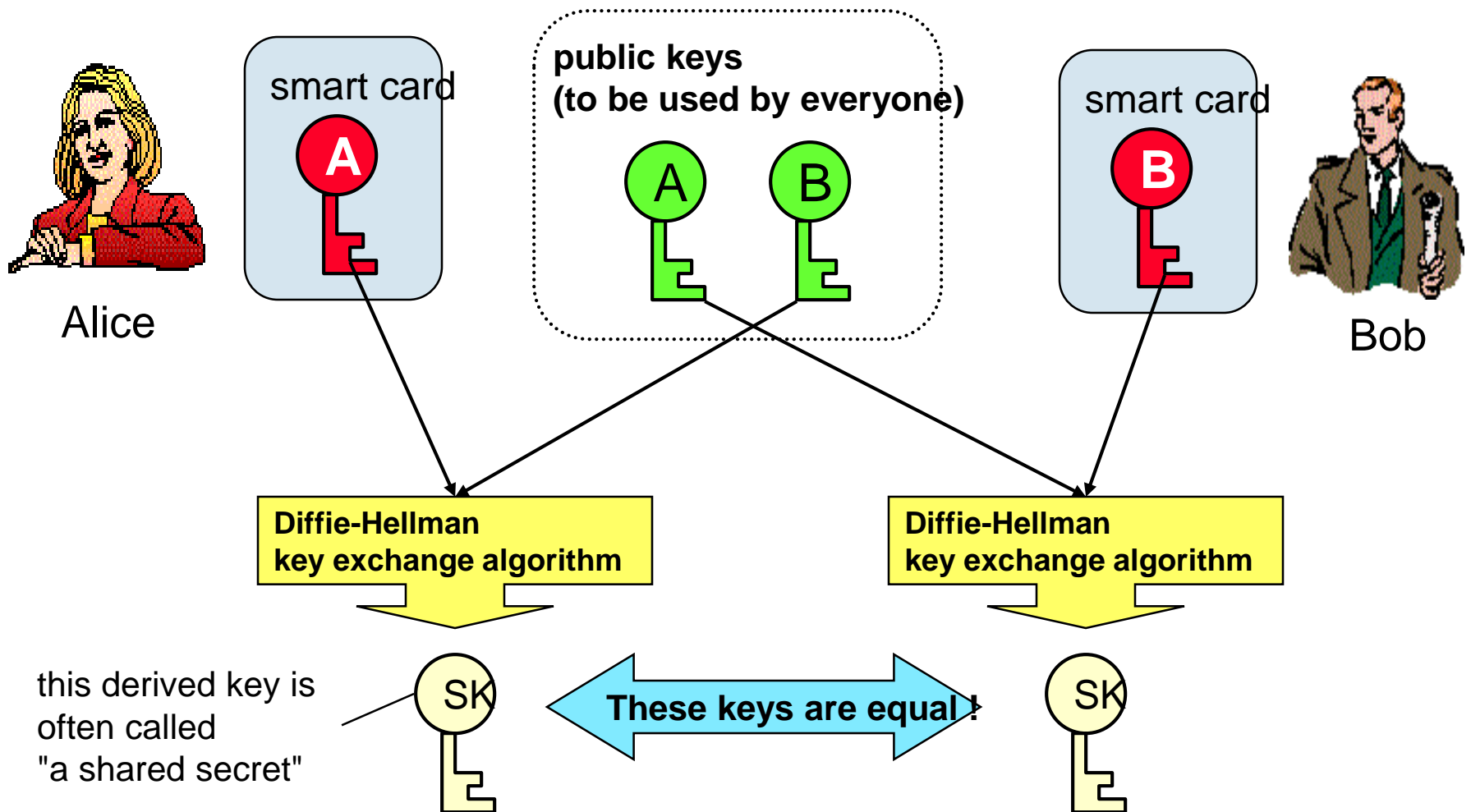
How to exchange the
common symmetric key
for hybrid encryption?

Two Solutions:

- Solution 1: By sending an encrypted symmetric key
- Solution 2: Using the Diffie-Hellman key exchange algorithm
--> next slide

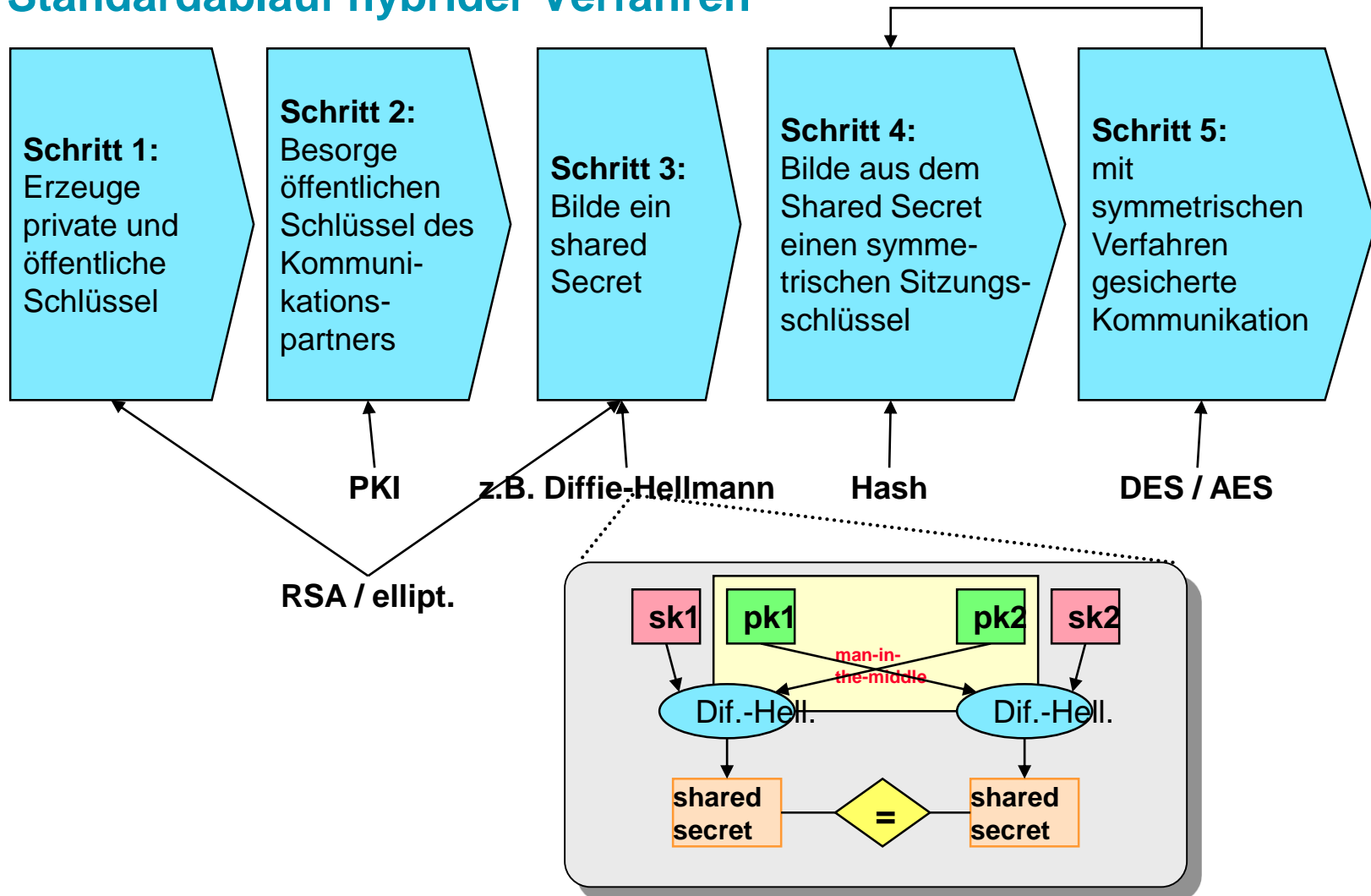


Diffie-Hellman Key Exchange Algorithm





Standardablauf hybrider Verfahren





hash function (one way function)

- plain text of arbitrary length is mapped to a hash value of fixed length
- It is difficult to find any (x, y) with $H(x) = H(y)$ (strong collision resistant)
- Given x it is difficult to find a y such that $H(x) = H(y)$ (weak collision resistant)
- MD5: 128 Bit hash value (used by PGP, not secure)
- SHA-1: 160 Bit hash value (attacked 2005 , not secure)
- SHA-2: set of hash functions (similar to SHA 1, secure)
- SHA-3: set of hash functions (alternative, dissimilar to SHA 1/2)
- RIPE-MD: 160 Bit hash value (is supposed to be very save)
- Message Authentication Code (MAC) ist eine schlüsselabhängige Einweg-Hashfunktion (→ Integrität + Authentizität der Nachricht), Realisierung durch DES oder AES im CBC-Mode



digital signature

- **Method:**
Hash the document D , encrypt the hash value H using the secret key S
→ the signed document = $(D, \text{enc}_S(H))$
- **Standards for digital signetures:**
 - DSA (Digital Signature Algorithm, diskreter Algorithmus, 1024-Bit Schlüssellänge,
 - NIST-Standard (National Institute of Standards and Technology)),
 - DSS (Digital Signature Standard, Nachfolger DSA, digitalen Beglaubigungsstandard der US-Regierung), RSA (einfacher und beliebter)



Erzeugung von sicheren Zufallszahlen

- Zufallszahlen werden zur Realisierung sicherer Protokolle benötigt
- Die Erzeugung von *echten* Zufallszahlen ist schwierig und mit algorithmischen Verfahren unmöglich:

John von Neumann:

Anyone who considers arithmetical methods of producing random digits is, of course, in a state of sin.

- jeder „Zufallszahlen“-Generator in einem Computer ist zwangsläufig periodisch und damit nicht zufällig
- Definition:
Ein Pseudozufallsbitgenerator ist ein deterministischer Algorithmus, der als Eingabe eine echt zufällige Bitfolge (seed) erhält und daraus eine (längere) Bitfolge erzeugt, die den *Eindruck der Zufälligkeit* erweckt.
- Die Güte eines Pseudozufallsbitgenerator kann mathematisch gefasst werden → kryptographisch sicherer Pseudozufallsbitgenerator